

Relació Partícules - Corrents

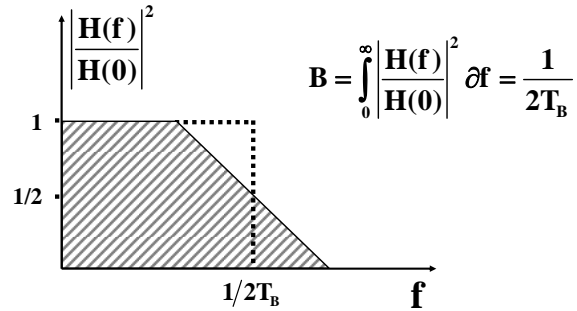
$$\langle s \rangle = \langle m \rangle + \langle p \rangle = \eta \langle n \rangle + \langle p \rangle \longrightarrow \text{Soroll Tèrmic} \quad \langle p \rangle = \frac{I_T T_B}{q}$$



Soroll Shot $\langle n \rangle = \frac{P T_B}{hf}$

$$\begin{cases} I_T = 0 \\ \sigma_T^2 = \frac{4KT_B}{R_L} \end{cases} \quad \begin{cases} \langle p \rangle = 0 \\ \sigma_p^2 = \left(\frac{T_B}{q}\right)^2 \frac{4KT_B}{R_L} \end{cases}$$

$$\begin{cases} \langle m \rangle \equiv M\eta \langle n \rangle \\ \sigma_m^2 \equiv M^2 F \eta \langle n \rangle \end{cases}$$



$$\begin{cases} I = M\mathcal{R}P = M\eta \frac{q}{hf} P = \frac{q}{T_B} M\eta \langle n \rangle \end{cases}$$

$$\begin{cases} \sigma_I^2 = 2qBM^2F(M)\mathcal{R}P = \frac{q}{T_B} M^2F(M)\eta \frac{q}{hf} P = \left(\frac{q}{T_B}\right)^2 M^2F(M)\eta \langle n \rangle \end{cases}$$

Sensibilitat del Receptor

$$\begin{aligned} \langle s \rangle &\equiv M\eta \langle n \rangle & I &= M\mathcal{R}P & \text{Estadística} \\ \sigma_s^2 &\equiv M^2 F \eta \langle n \rangle + \sigma_p^2 & \sigma_I^2 &= 2qBM^2F(M)\mathcal{R}P + \sigma_T^2 & \text{Gaussiana} \end{aligned}$$

$$Q \equiv \frac{I_1 - I_0}{\sigma_1 + \sigma_0} = \frac{M\mathcal{R}P_1}{\sqrt{2qBM^2F(M)\mathcal{R}P_1 + \sigma_T^2 + \sigma_T}} \quad \bar{P} \equiv \frac{1}{2}(P_1 + P_0)$$

$$\frac{M\mathcal{R}P_1}{\sqrt{2qBM^2F(M)\mathcal{R}P_1 + \sigma_T^2 + \sigma_T}} \geq 6 \longrightarrow \bar{P} \geq 36qB \frac{F(M)}{\mathcal{R}} + 6 \frac{\sigma_T}{M\mathcal{R}} \equiv S$$

$$F(M) = M^x$$

$$S_{PIN} = 36q \frac{B}{\mathcal{R}} + 6 \frac{\sigma_T}{\mathcal{R}} \approx 6 \frac{\sigma_T}{\mathcal{R}} \quad \text{Domini Tèrmic}$$

$$\frac{\partial S}{\partial M} = 36xqB \frac{M^{x-1}}{\mathcal{R}} - 6 \frac{\sigma_T}{M^2\mathcal{R}} = 0 \longrightarrow M_{OPT}^{x+1} = \frac{\sigma_T}{6xqB} \longrightarrow S_{OPT}$$